

UNIVERSITY OF THE PUNJAB

B.S. 4 Years Program : First Semester - Fall 2021

Paper: Statistics-I Course Code: STAT-101

Roll No.

Time: 3 Hrs. Marks: 60

Q.1. Answer the following short questions.

(15x2=30)

- (i) Define Descriptive and Inferential statistics
- (ii) Define a variable. Differentiate between discrete and a continuous variable.
- (iii) What is meant by frequency distribution and cumulative frequency distribution.
- (iv) Define the statistical term histogram and frequency polygon.
- (v) What is a measure of central tendency? What are its desirable qualities?
- (vi) Show that $\sum (x_i \overline{x}) = 0$
- (vii) What is coefficient of variation? What purpose does it serve?
- (viii) The first four moments of a distribution about x=2 are 1,2.5, 5.5 and 16 calculate the first four moments about mean and calculate β_1 and β_2
- (ix) Compare the simple aggregative and weighted aggregative index numbers.
- (x) Prove that fisher's ideal index satisfies the factor reversal test.
- (xi) Show that standard deviation of regression $sy.x = \sqrt{\frac{\sum y^2 a\sum y b\sum xy}{n-2}}$
- (xii) Define rank correlation, which quantity is added to $\sum d^2$ for tied ranks.
- (xiii) What is meant by coefficient of determination?
- (xiv) Distinguish between the secular and seasonal variation in time series analysis.
- (xv) Define detrending and deseasonlization.

Solve the following questions.

Q:2 (a) The following data relate to size of shoes sold at a store during a given week. Find the median and the model size of shoes also find D_9 and P_{70} . (6+4=10)

| Size of Shoes | 5 | $5\frac{1}{2}$ | 6 | $6\frac{1}{2}$ | 7 | $7\frac{1}{2}$ | 8 | $8\frac{1}{2}$ | 9 | $9\frac{1}{2}$ |
|------------------|---|----------------|----|----------------|----|----------------|----|----------------|---|----------------|
| No of Pairs | 3 | 7 | 20 | 30 | 60 | 50 | 25 | 17 | 8 | 2 |

(b) Show that var(x+a) = var(x) where 'a' is some constant.

Q:3 (a) Show that correlation coefficient is independent of change of origin and scale i.e $r_{xy} = r_{uv}$ if

$$u = \frac{x-a}{h}, v = \frac{y-b}{k}$$
 (4+6=10)

(b) Construct fisher's ideal index number for 2011, taking 2010 as base

| Items | Quantity | | Value | | | |
|-------|----------|------|-------|------|--|--|
| | 2010 | 2011 | 2010 | 2011 | | |
| A | 110 | 175 | 600 | 1000 | | |
| В | 90 | 120 | 400 | 800 | | |
| С | 70 | 85 | 200 | 350 | | |

Q:4 (a) Compute the seasonal indices by ratio to trend method using least square line y=119.56+2.76x by taking origin in the centre and unit of x being half quarter.

(b) Deseasonlize the values of years 1999 and 2000

(7+3=10)

| QUARTERS | | | | | |
|----------|-----|-----|-----|-----|--|
| Year | I | п | Ш | IV | |
| 1997 | 72 | 98 | 79 | 106 | |
| 1998 | 79 | 122 | 101 | 143 | |
| 1999 | 94 | 141 | 128 | 160 | |
| 2000 | 125 | 143 | 135 | 187 | |