UNIVERSITY OF THE PUNJAB

B.S. 4 Years Program / First Semester – Spring 2023

Paper: Mathematics A-I [Calculus(I)] Course Code: MATH-101

Roll No.

Time: 3 Hrs. Marks: 60

THE ANSWERS MUST BE ATTEMPTED ON THE ANSWER SHEET PROVIDED

Q.1. Solve the following:

(6x5=30)

(i)	Using the concept of shifting and scaling of functions, draw the graph of $y = (x + 1)^2 - 1$	(5)
(ii)	Find the limit of: $\lim_{x\to 5} \left(\frac{x-5}{x^2-25}\right)$.	(5)
(iii)	Find the values of x for which $f(x)$ is continuous $f(x) = \frac{x^2 + x - 6}{x^2 - 4}$.	(5) ¹
(iv)	Find derivative of $f(x)$ if $f(x) = \ln(2x) + 1$.	(5)
(v)	Solve the inequality: $ 2 - 3x > 5$.	(5)
(vi)	Evaluate the Integral $\int \left(\frac{x^9}{2} + \frac{2}{\sqrt{x}}\right) dx$.	(5)

Solve the following:

(5x6=30)

Q.2	Find derivative w.r.t 'x' of $\ln \sqrt{\tan^{-1} 2x}$.	(6)
Q.3	Solve the integral $\int \sin(2+x^3)x^5dx$.	(6)
Q.4	If $y = tan^{-1}x$, show that $(1+x^2)y'' + 2xy' = 0$. Hence find the value of $y^{(n)}(x)$.	(6)
Q.5	Find the limit by using L'Hopital's rule: $\lim_{t\to 0} \left(\frac{1-\cos t}{t^2}\right)$.	(6)
Q.6	Using intermediate value theorem, show that the equation $x^3 + 3x + 1 = 0$, has exactly one real solution.	(6)