Module Code: MATH-429

Module Title: Functional Analysis - III

Module Rating: 3 Cr. Hours

Pre-Requisite: Functional Analysis - I

### Semi-norms

- Semi norms, locally convex Spaces
- Quasi normed linear spaces
- Bounded linear functionals
- Hahn Banach theorem

# Conjugate spaces

- Second conjugate space of l<sub>p</sub>
- The Riesz representation theorem for linear functionals on a Hilbert spaces
- Conjugate space of C[a,b]
- A representation theorem for bounded linear functionals on C[a,b]

### **Uniform Boundedness**

- Weak convergence
- The Principle of uniform boundedness
- Consequences of the principle of uniform boundedness
- Graph of a mapping and closed graph theorem

## Linear transformation and complete continuity

- The closure of linear transformation
- The class of linear transformations that admit a closure

#### Recommended Books

- 1. G. Bachman and L. Narici, Functional Analysis, (Academic Press, New York, 1966)
- 2. A. E. Taylor, Functional Analysis, (John Wiley and Sons, Toppan, 1958)
- 3. G. Helmberg, *Introduction to Spectral theory in Hilbert spaces*, (N. H. Publishing Company 1969)
- 4. E. Kreyszig, *Introduction to Functional Analysis with Applications*, (John Wiley and Sons, 2004)
- 5. F. Riesz and B. Sz. Nagay, Functional Analysis, (Dover Publications, New York, Ungar, 1965)
- 6. W. Rudin, Functional Analysis, 2<sup>nd</sup> edition, (McGraw Hill Book Company, New York, 1991)