Course Title: Numerical Methods with Computer Programming

Course Code: MATH-406

Course Type: Major Math

Prerequisites: Numerical Analysis & Computational Tools

Credit Hours: 3 (3 + 0)

Course Objectives: After the completion of the course, students will be able to:

- Extend knowledge of numerical methods to differential equations, difference equations and advanced integration techniques.
- Explore numerical differentiation and integration.
- Understand ordinary differential equations using numerical methods.
- Study the formulation and solution of difference equations.
- Apply numerical methods to solve ordinary differential equations.

Course Contents:

Numerical Differentiation: Derivatives using Lagrange's interpolation formula, Newton's divided difference formula, Gregory Newton's forward/backward interpolation formula, Gauss's forward/backward interpolation formula, Stirling's formula, Laplace Everett's formula, Bessel's formula. Lab Work: In MATLAB / Mathematica / Python.

Numerical Integration: Newton-Cotes formulae, Trapezoidal rule, Simpson rule, Weddle's rule, Boole's rule, Errors in quadrature formulae, Gaussian quadrature formulae. Lab Work: In MATLAB / Mathematica / Python.

Formulation of Difference Equations: Analogy of difference equations, Linear homogeneous difference equations with constant coefficients, Linear non-homogeneous difference equations with constant coefficients.

Numerical Methods for Ordinary Differential Equations: Solutions of first order differential equations, Simultaneous first order differential equations, Higher order differential equations using Taylor's series method, Euler's method, Improved Euler's method, Modified Euler's method and Runge-Kutta methods, Predictor-corrector methods for solving initial value problems. Lab Work: In MATLAB / Mathematica/ Python.

Recommended Books:

- 1. Burden, R. L. and Faires, J. D., Numerical Analysis, Cengage Learning, 10th edition, 2015.
- 2. Chapra, S. C. and Canale, R. P., *Numerical Methods for Engineers*, McGraw Hill, 7th edition, 2014.
- 3. Gerald, C. F. and Wheatley, P. O., *Applied Numerical Analysis*, Pearson College Div., 7th edition, 2003.

- 4. Mathews, J. H., Numerical Methods for Mathematics, Pearson College Div., 1992.
- 5. Vedamurthy, V. N. and Iyenger, N. Ch. S. N., *Numerical Methods*, Vikas Publishing House Pvt. Ltd, 2002.
