

The invariable boundary conditions are:

$$\widehat{f}_n(0) = \widehat{f}'_n(0) = \widehat{\theta}_n(0) = \widehat{\phi}_n(0) = 0, \quad \widehat{f}''_n(\beta) = \widehat{\theta}'_n(\beta) = \widehat{\phi}'_n(\beta) = 0 \quad (3.52)$$

Here

$$\begin{aligned} R_n^f(\eta) = & (1+k)\widehat{f}''''_{n-1} - \sum_{k=0}^{n-1} \widehat{f}'_{n-1-k} \widehat{f}'_k + \sum_{k=0}^{n-1} \widehat{f}_{n-1-k} \widehat{f}''_k - A \left[\widehat{f}'_{n-1} + \frac{\eta}{2} \widehat{f}''_{n-1} \right] \\ & + \lambda \sum_{k=0}^{n-1} \left(\widehat{f}''_{n-1-k} \right)^2 \widehat{f}'''_k - M \widehat{f}'_{n-1} - k^* \widehat{f}'_{n-1}. \end{aligned} \quad (3.53)$$

$$\begin{aligned} R_n^\theta(\eta) = & (1+\xi\theta) \widehat{\theta}''_{n-1} + \frac{1}{Pr} \xi \sum_{k=0}^{n-1} \widehat{\theta}_{n-1-k} \widehat{\theta}''_k + \sum_{k=0}^{n-1} \widehat{f}_{n-1-k} \widehat{\theta}'_k - 2 \sum_{k=0}^{n-1} \widehat{f}'_{n-1-k} \widehat{\theta}_k \\ & - \frac{A}{2} \left(3\widehat{\theta}_{n-1} + \eta \widehat{\theta}'_{n-1} \right) + Nb \sum_{k=1}^{n-1} \widehat{\theta}'_{n-1-k} \widehat{\phi}'_k + Nt \sum_{k=1}^{n-1} \widehat{\theta}'_{n-1-k} \widehat{\theta}'_k. \end{aligned} \quad (3.54)$$

$$\begin{aligned} R_n^\phi(\eta) = & \widehat{\phi}''_{n-1} + Sc \sum_{k=0}^{n-1} \widehat{f}_{n-1-k} \widehat{\phi}'_k - 2Sc \sum_{k=0}^{n-1} \widehat{f}'_{n-1-k} \widehat{\phi}_k - \frac{A Sc}{2} \left(3\widehat{\phi}_{n-1} + \eta \widehat{\phi}'_{n-1} \right) \\ & + \frac{Nt}{Nb} \widehat{\theta}''_{n-1} \end{aligned} \quad (3.55)$$

Where

$$\chi_n = \begin{cases} 1, & \zeta > 1 \\ 0, & \zeta \leq 1 \end{cases} \quad (3.56)$$

4. CONVERGENCE:

When we computed the series solutions of velocity, temperature and concentration functions using HAM, the assisting parameters $h_{f,\theta}$ and h_ϕ appears, which are responsible for adjusting the convergence of solutions. h-curve graphs of $f''(0), \theta'(0)$ and $\phi'(0)$ for 7th order Approximation are plotted to get the possible region of h curve in the Figures (2-3) for various values of embedded variables. The h-curves consecutively display the valid region. The convergence region of the h-curve in Figs. 2 and 3 is shown as $-0.2 \leq h \leq 0.0$ which is a valid region.

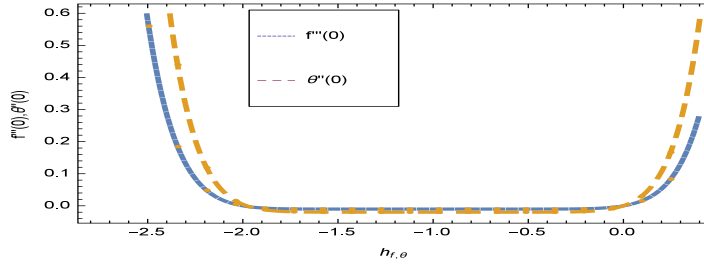


FIGURE 2. Combine h curve of function f and θ at 7^{th} order approximation, when $\gamma = Sc = A = \xi = \beta = k = 0.1, Nb = Nt = 0.3, M = Pr = 1$.

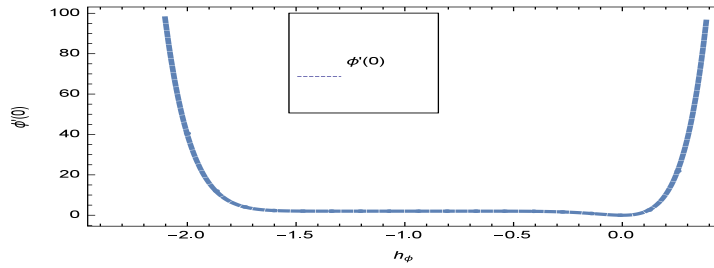


FIGURE 3. The h curve function of ϕ for 7^{th} order approximation, when $\gamma = Sc = A = \xi = \beta = k = 0.1, Nb = Nt = 0.3, M = Pr = 1$.

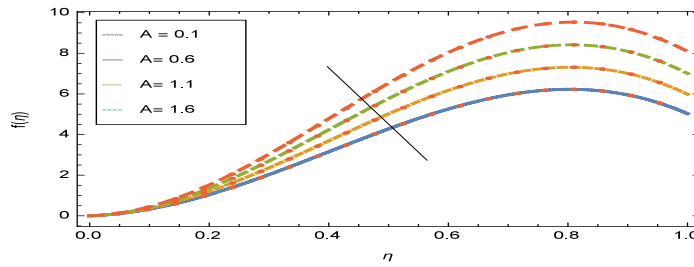


FIGURE 4. Influence of A on $f(\eta)$, where $\beta = 0.4, M = 1, \gamma = 0.7, \lambda = k = 0.6$.

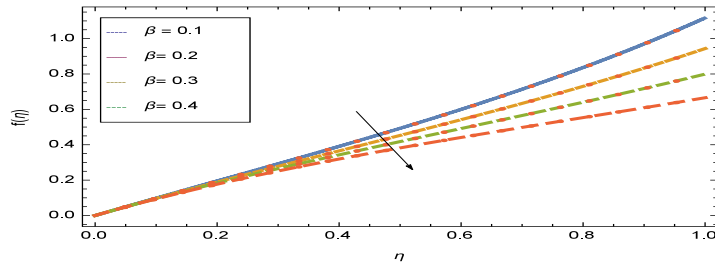


FIGURE 5. Influence of β on $f(\eta)$, where $A = 0.1, M = 1, \gamma = 0.7, \lambda = k = 0.6$.

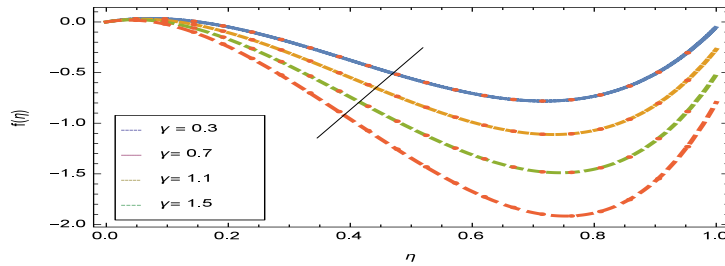


FIGURE 6. Influence of γ on $f(\eta)$, where $\beta = 0.4, M = 1, A = 0.9, \lambda = 0.5, k = 0.6$.

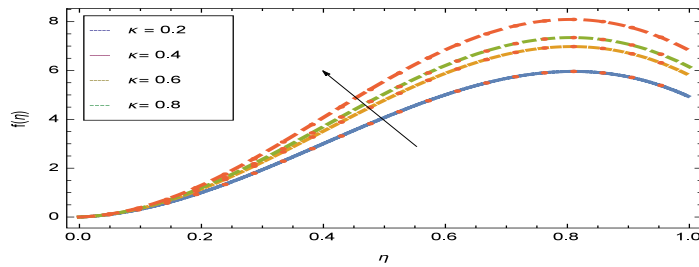


FIGURE 7. Influence of k on $f(\eta)$, where $\beta = 0.4, M = 1, A = 0.9, \lambda = \gamma = 0.5$.

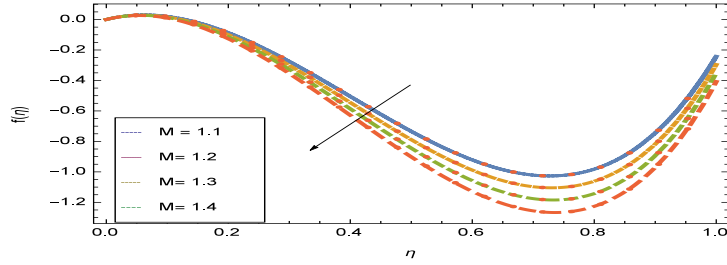


FIGURE 8. Influence of M on $f(\eta)$, where $\beta = 0.4, \gamma = 0.7, \lambda = 0.3, A = 0.9, k = 0.6$.

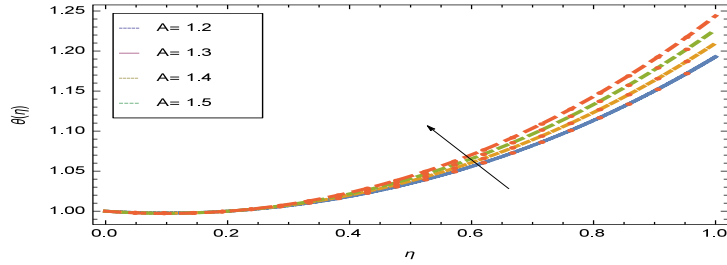


FIGURE 9. Influence of A on $\theta(\eta)$, where $\gamma = Sc = \xi = 0.6, \beta = 0.1, Nb = 0.3, M = 0.5, Nt = k = 0.4, Pr = 1$.

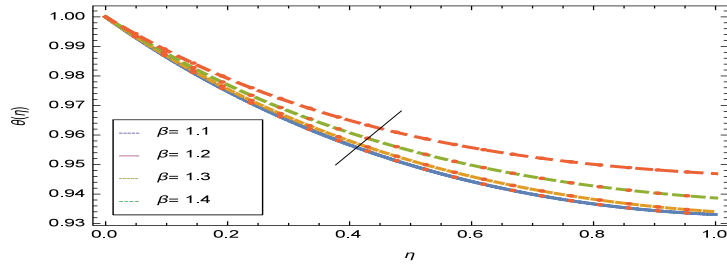


FIGURE 10. Influence of β on $\theta(\eta)$, where $\gamma = A = Sc = \xi = 0.6, M = 0.1, Nb = 0.3, Nt = k = 0.4, Pr = 1$.

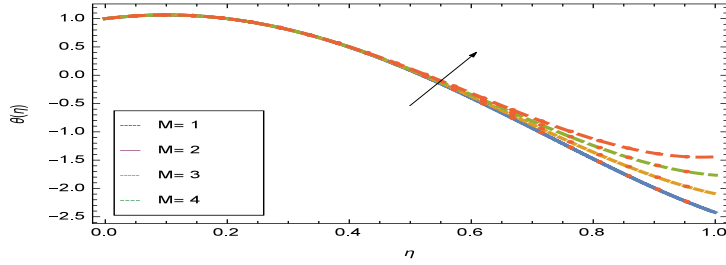


FIGURE 11. Influence of M on $\theta(\eta)$, where $\gamma = A = Sc = \xi = 0.6, \beta = 0.1, Nb = 0.3, Nt = k = 0.4, Pr = 1$.

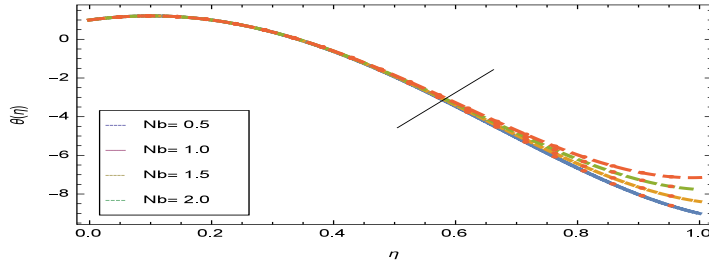


FIGURE 12. Influence of Nb on $\theta(\eta)$, where $\gamma = A = Sc = \xi = 0.6, \beta = 0.1, M = 0.5, Nt = Rd = k = 0.4, Pr = 1$.

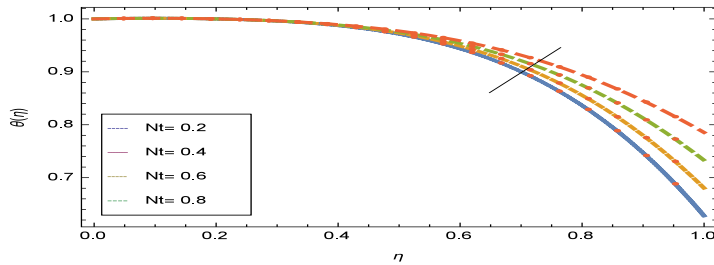


FIGURE 13. Influence of Nt on $\theta(\eta)$, where $\gamma = A = Sc = \xi = 0.6, \beta = 0.1, M = 0.5, Nb = 0.3, Rd = k = 0.4, Pr = 1$.

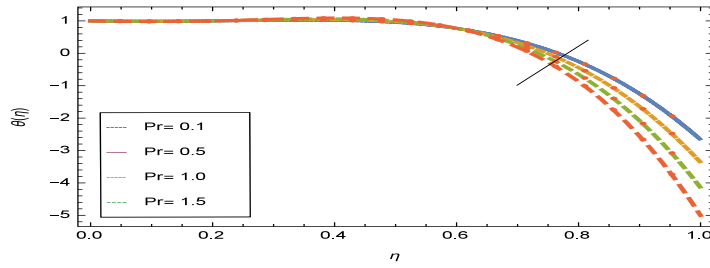


FIGURE 14. Influence of Pr on $\theta(\eta)$, where $\gamma = A = Sc = \xi = 0.6, \beta = 0.1, M = 5, Nb = 3, Nt = Rd = k = 0.4$.

FIGURE 15. Influence of Sc on $\theta(\eta)$, where $\gamma = A = \xi = 0.6, \beta = 0.1, M = 0.2, Nb = 0.3, Nt = k = 0.4, Pr = 1$.

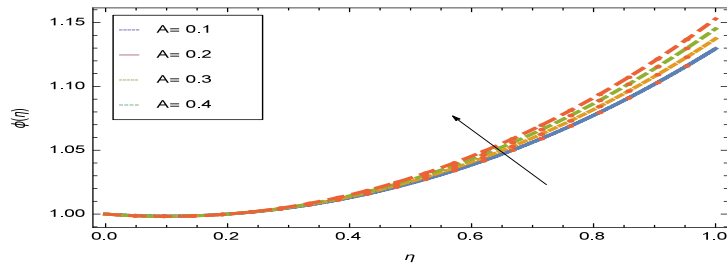


FIGURE 16. Influence of A on $\phi(\eta)$, where $\gamma = Sc = \xi = 0.6, \beta = 0.1, M = 0.5, Nb = 0.3, Nt = k = 0.4, Pr = 1$.

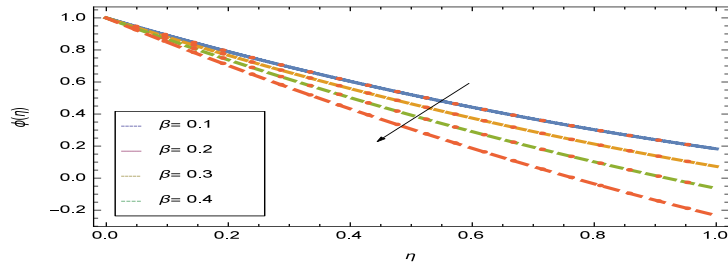


FIGURE 17. Influence of β on $\phi(\eta)$, where $\gamma = 1.9, Sc = 0.3, \xi = 1.1, M = 0.2, Nb = 0.5, A = 1.2, Nt = 0.5, k = Pr = 0.1$.

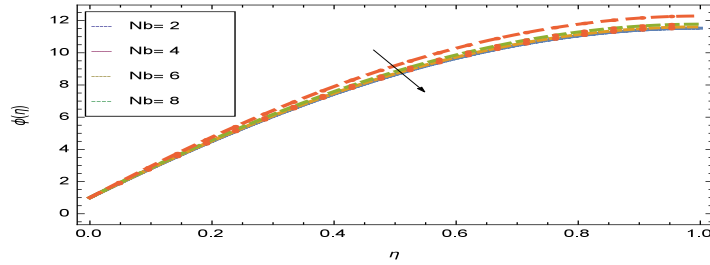


FIGURE 18. Influence of Nb on $\phi(\eta)$, where $\gamma = Sc = \xi = 0.6, \beta = 1, M = 0.1, A = 0.5, Nt = k = 0.4, Pr = 1$.

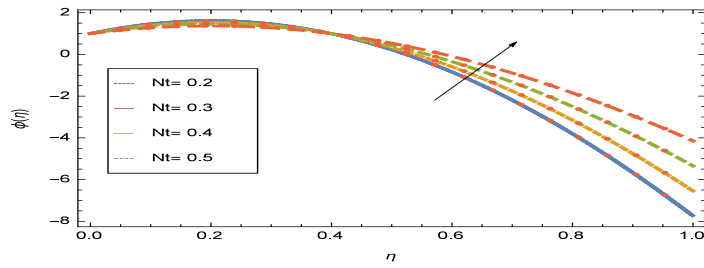


FIGURE 19. Influence of Nt on $\phi(\eta)$, where $\gamma = Sc = \xi = 0.6$, $\beta = 0.2, M = 0.1, Nb = A = 0.5, k = 0.5, Pr = 1$.

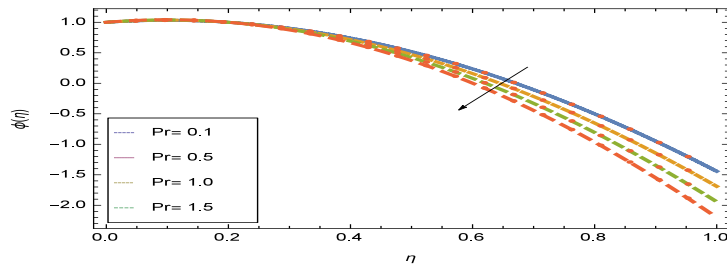


FIGURE 20. Influence of Pr on $\phi(\eta)$, where $\gamma = Sc = A = \xi = 0.6, \beta = 0.1, M = Nb = Nt = 0.5, k = 0.4$.

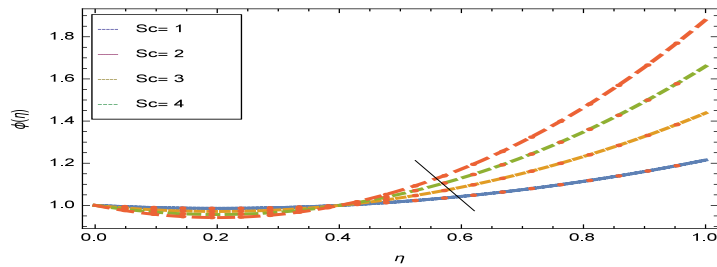


FIGURE 21. Influence of Sc on $\phi(\eta)$, where $\gamma = \xi = 0.6, \beta = 0.2, M = 0.1, Nb = A = 0.5, Nt = k = 0.4, Pr = 1$.

5. TABLES DISCUSSION

This section is about the discussion of tables. Table.1 displays numerical values of HAM solutions at different approximation using different values for various parameters. Clearly the table values shows that homotopy analysis technique is a quickly convergent technique. Table quantities such as film thickness β , skin friction co-efficient $f''(0)$, heat flux $Nu = -\theta'(0)$ and mass flux $Sh = -\phi'(0)$ for engineering interest are calculated from Tables 2,3 and 4. In Table.2 values of skin friction co-efficient $f''(0)$ and thin film thickness β are determined using increasing values of A. It is analyzed that skin friction co-efficient increases and the thin film thickness reduces randomly with increasing values of A. In table.3 the effect of M, Nt, A and Pr on wall temperature is calculated taking $A = 0.8$ the large value of M and Nt increase the wall temperature while the large value of A and Pr reduces the wall temperature. Table.4 examines the effect of embedding parameters Nb, β , Pr and Nt on the heat flux $Nu = -\theta'(0)$ and mass flux $Sh = -\phi'(0)$. It has been seen that the increasing values of Nb, β and Pr decreases mass flux while the increasing values of Nt increases mass flux. It has also been seen that the increasing values of embedded parameters randomly varies heat flux. The current results of $-\theta'(0)$ and $-\phi'(0)$ having a resemblance in appearance.

Table 1. Convergence of $f''(0)$, $\theta'(0)$ and $\phi'(0)$ by HAM Method when $Nt = Nb = 0.3, A = Sc = k = \xi = \gamma = \beta = 0.1, Pr = M = 1$.

Solution Approximation	$f''(0)$	$\theta'(0)$	$\phi'(0)$
1	-0.05401	-0.10070	-1.10075
4	-0.10218	-0.18890	-1.38506
7	-0.10813	-0.19903	-1.88867
10	-0.10888	-0.20281	-1.99293
13	-0.10894	-0.20154	-2.01113
14	-0.10896	-0.20475	-2.01406
17	-0.10897	-0.20478	-2.01451
20	-0.10897	-0.20479	-2.01458
25	-0.10897	-0.20479	-2.01458

Table 2. Results of skin friction coefficient $f''(0)$ and film thickness β for various values of A.

A	Present Results $f''(0)$	Present Results β
0.4	-4.33027	5.523451
0.6	-3.94882	4.002111
0.8	-2.64208	3.992358
1.0	-1.33999	3.113001
1.2	-0.92157	1.625391
1.4	-0.56897	1.896541
1.6	-0.34227	0.876512
1.8	-0.03027	0.266156

Table 3. The wall temperature for dissimilar values of M, A, Pr and Nt when $A = 0.8, Nb = 0.4, \beta = 0.9, Nb = 1.6$

M	Nt	A	Pr	Present (2017) Results $\theta(\beta)$
0	0.1	1.0	0.1	0.223456
1				0.432111
2	0.01			0.712351
	0.1	0.0		1.023001
		1.0	0.1	1.625341
			0.2	1.236540

Table 4. The Nusslet number $\phi'(0)$ and Sherwood numbers $\theta'(0)$ verses various value of embedded parameters when $A = 0.8$.

Nb	β	Pr	Nt	$-\theta'(0)$ Present Results	$-\phi'(0)$ Present Results
0.0	0.2	1.0	0.1	0.682385	6.68238
0.5				0.541422	4.94142
1.0				0.440569	5.44569
	0.2			0.321022	5.12101
	0.3			0.300420	5.70742
	0.4			0.291420	5.29140
		0.5		0.371420	5.37143
		1.5		0.182285	6.78223
		5.0		0.011422	7.01147
			0.4	0.612427	4.11207
			0.6	0.691428	4.69458
			0.8	0.500987	7.50097

6. DISCUSSION:

The present work focuses on the comprehension of the fluid film motion through modeled parameters. The graphical explanation of these parameters have been illustrated in figures [4-21] while Fig.2 is the combine h curve graph of velocity and temperature profiles and Fig.3 is the h curve graph of concentration profile. Both the graphs reflect valid region which gaurantees that homotopy analysis method is fast convergent technique. The influence of unsteady constraint A on the $\hat{f}(\eta)$ field shown in Fig.4. The velocity profile $\hat{f}(\eta)$ rises with the rise in A . Velocity increases with the unsteady constraint A . The influence of film thickness β has been displayed for unlike values of fluid velocity in Fig.5. It is observed that $\hat{f}(\eta)$ falls over with greater values of β . The impact of stretching parameter γ on the $\hat{f}(\eta)$ has been shown in Fig.6. It has been seen that $\hat{f}(\eta)$ decreases with the

growing values of stretching parameter. The effect of Eyring fluid factor k over the $\hat{f}(\eta)$ is exposed in Fig.7. It has been seen, when Eyring fluid parameter k increases then it increases the nanofluid film motion, and this influence is clear at the stretching surface. The characteristics of magnetic factor M on fluid velocity and heat profile are shown in Figs.8 and 11. It is obvious from mathematical formulation that M is inversely varied with velocity field $\hat{f}(\eta)$. Increasing M decreases the velocity field. This effect of magnetic field is caused by the production of friction force to the movement known as Lorentz force which bring retardation to the flow of the fluid and hence decreases fluid velocity at the upper surface. It is clear from Fig.16 that all the fluids reflect the similar reaction to the unsteady parameter. The slope in the temperature distribution falls down with decreasing the width of thermal boundary layers. It means that unsteady parameter A has inverse effect on the temperature field. Fig.9. shows that heat profile decreases with the parameter A . Every fluid observes the same effect on temperature profile for parameter A . Actually, the fluid produces resistance to the flow of film and shows a tendency to decay the velocity of fluid flow having greater values of β and it is obvious in Fig.11. The fluid film size absorbs heat that causes falls down in heat distribution. The free surface temperature is increased with the Brownian motion constraint as illustrated in Fig.12. The reality is that the random movement of molecules of fluid produces collisions among the molecules. Increase in the value of Brownian motion parameter Nb , results increase in temperature of the fluid, consequently, it causes reduction in free surface nanoparticle volume fraction and is shown in Fig.18. The thermophoresis parameter Nt decreases as the temperature profile increases and it can be seen in Fig.13. The thermophoresis constraint is responsible for raise in surface temperature. The random motion of nano particles of fluid produces Brownian motion. This irregular motion of nano suspended particles is responsible for kinetic energy and it causes rise in temperature. Consequently, thermophoretic force is produced. This force produces intensity in the fluid to move away from the surface of the stretching sheet. Subsequently, the temperature inside the boundary layer rises as Nt increases. Physically, the Prandtl number is the ratio of kinematic viscosity to thermal diffusivity and is a dimensionless quantity. The value of Pr is increased if the value of thermal diffusivity is less than the momentum diffusivity. Therefore, the heat transmission at the exterior increases as the values of Pr increase while mass transmission reduces as the Prandtl number increases. The influence of Pr is shown in the Fig.14. It obviously shows that $\hat{\theta}(\eta)$ reduces with large Pr number. The logic behind is that the large value of Prandtl number reduces thermal layer of the boundary. The consequences are more prominent for minor Prandtl quantity because of relatively greater width of thermal boundary layer. The heat distribution $\hat{\theta}(\eta)$ increases with the change in the Schmidt number and is shown in Fig.15, and the non-dimensional concentration profile reduces with dissimilar measures of parameter Sc displayed in Fig.21. It is visible that a flow part increases in the horizontal direction by rising the Schmidt number. It clearly reflects that with rise in the Schmidt number, the flow part increases in the x-direction. The logic is that the Sc parameter is the ratio of momentum to the concentration diffusivities. The growth in Sc reduces width of fluid and causes fall down in $\hat{\theta}(\eta)$. The viscosity dissipation effect on the nanoparticle volume fraction is insignificant for higher quantities of Schmidt numbers. The concentration of the fluid $\hat{\phi}(\eta)$ increases as values of β grows as presented by Fig.17. The logic behind is that width of fluid film exhibit direct

proportion with thermal conductivity as well as with viscosity. As thermophoresis parameter Nt increases, concentration field elevates. Just like surface temperature, thermophoresis factor also help in increasing the exterior of nanoparticle volume fraction and is illustrated in Fig.19. The increasing values of Nt decrease the surface mass transfer rate in both steady and unsteady cases, but shows high mass transfer rate on external edge in unsteady case as compared to steady one. Concentration profile shows the inverse relation with Pr number as shown in Fig.20. It means thinning of thermal boundary layer increases flow in the x-direction, which is clearly exhibited in the graph.

7. CONCLUDING REMARKS:

This research work analyzes two dimensional nanofluid film flow of Eyring Powell Fluid with variable heat transmission over a porous stretching sheet in the existence of uniform magnetic field (MHD). The observation of this work depends upon the influence of variable temperature and magnetic field on nanofluid film flows. The influence of the skin fraction, Nusselt number and Sherwood number is shown numerically.

The key points of this work are as under:

- The increasing values of Pr increases the surface temperature, where opposite effect is found for unsteady parameter A that is the large values of A reduces the surface temperature.
- Non-dimensional velocity decline in variable viscosity and magnetic parameter.
- The temperature and concentration profile both are directly proportional with magnetic field.
- It is perceived that the large value of Magnetic parameter drops the velocity distribution of the nanofluid films.
- The larger values of Brownian motion parameter rises the profile of temperature.
- Thermal boundary layer thickness reduces with rise of Sc , Nusselt number rises with rise in Prandtl number.
- Porosity parameter decrease the motion of the liquid films.
- It is observed that the temperature profile falls with the large numbers of thermophoresis parameter Nt and increases for small values.
- Augmenting the nanoparticle concentration efficiently increases the friction feature of Eyring nanofluid.
- The increasing values of Nb reduces the mass flux, where Nt increases the mass flux. The higher values of Re reduces the mass flux, while it rises with rising values of Sc .
- The convergence of the HAM method with the variation of the physical parameters observed numerically.

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9. AUTHORCONTRIBUTIONS

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10. COMPETING INTERESTS

Authors have declared that no competing interests exist.

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